

the metric backbone of contact networks



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in Epidemic Spread Models

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Indiana University
Network Science Institute



FULBRIGHT

PERSISTENT

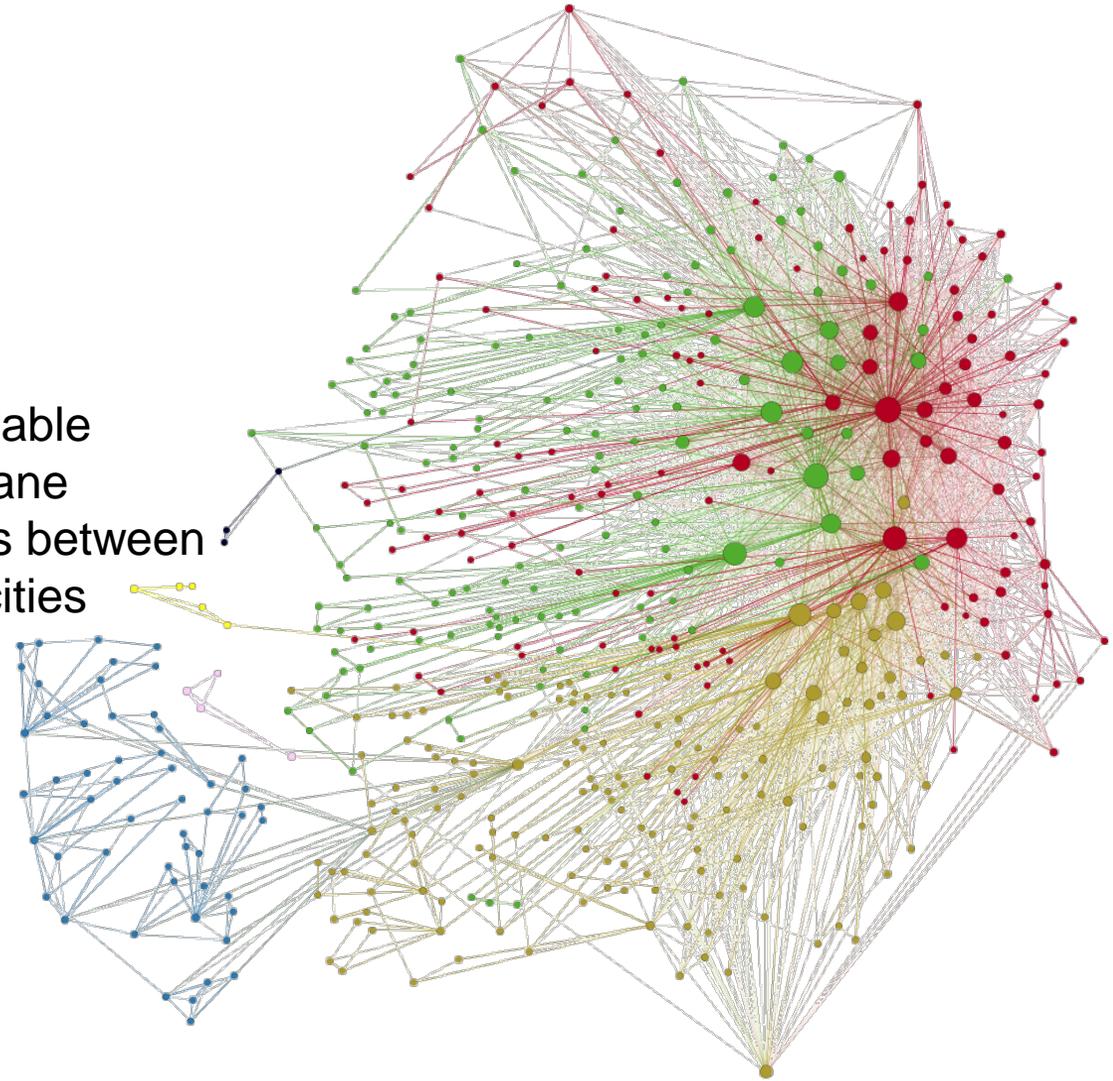
INDIANA UNIVERSITY

rocha@indiana.edu
<http://informatics.indiana.edu/rocha>

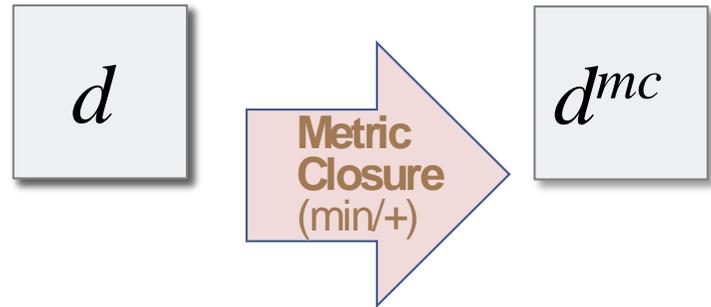
of distance networks (weighted graphs)

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Available
airplane
seats between
US cities

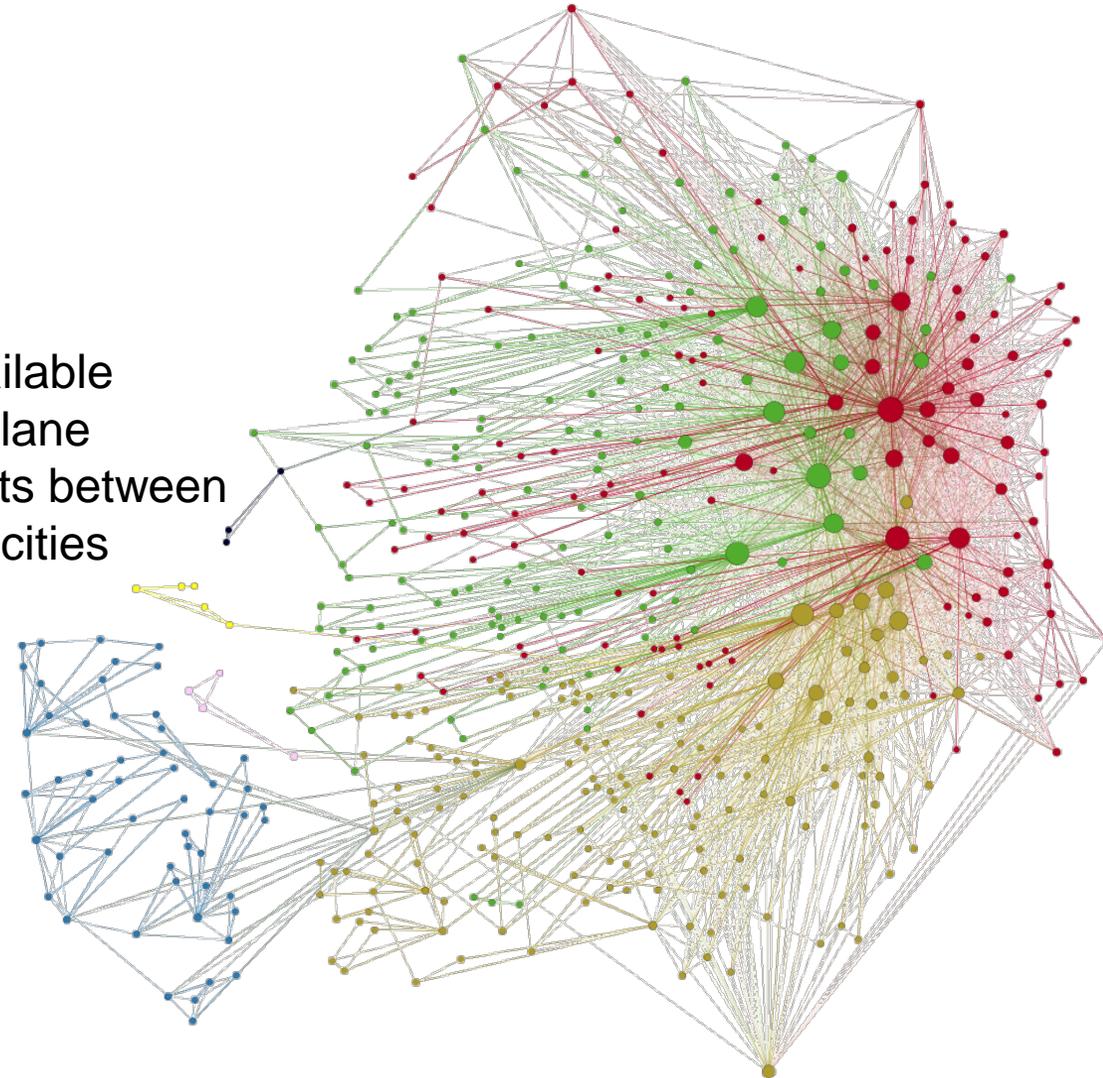


of distance networks (weighted graphs)



all pairs *shortest paths* problem
(APSP) on distance graphs

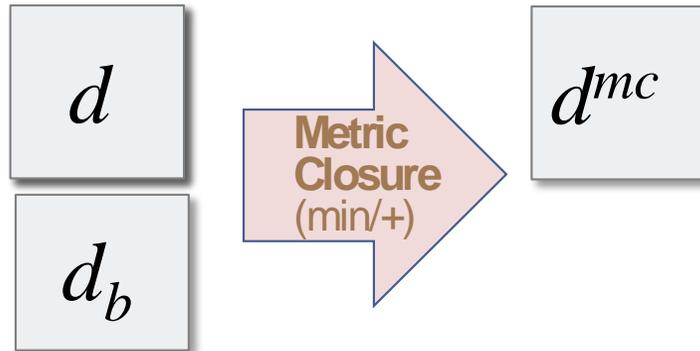
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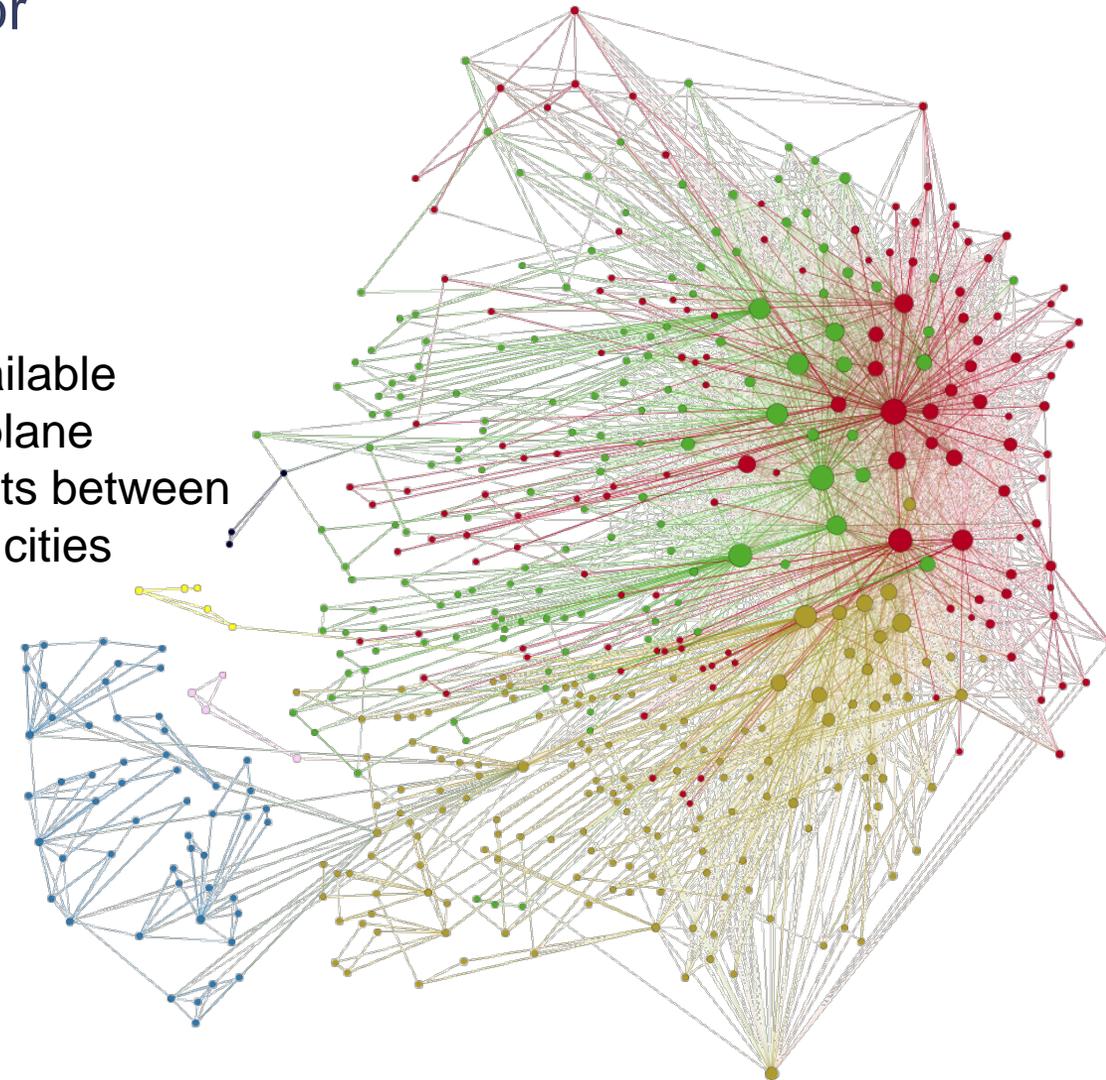
Metric (distance) Backbone: minimum sub-graph for which all shortest paths are preserved.

Invariant subgraph under metric closure (or APSP)



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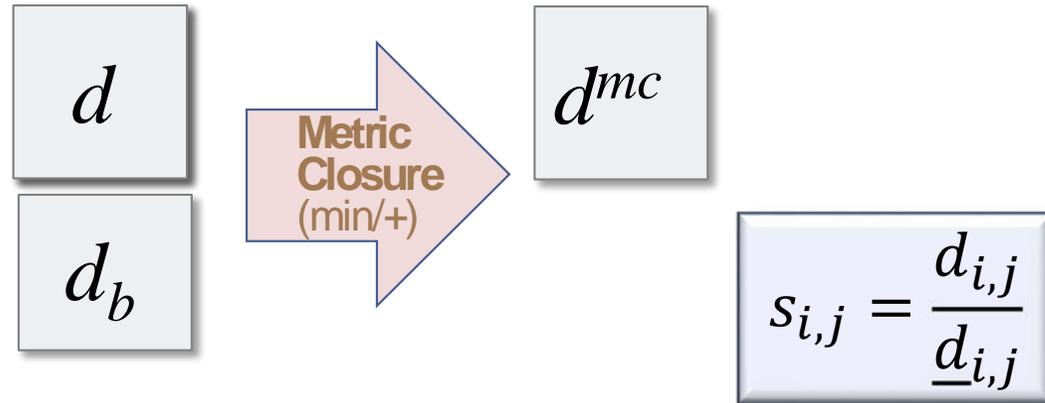


of distance networks (weighted graphs)

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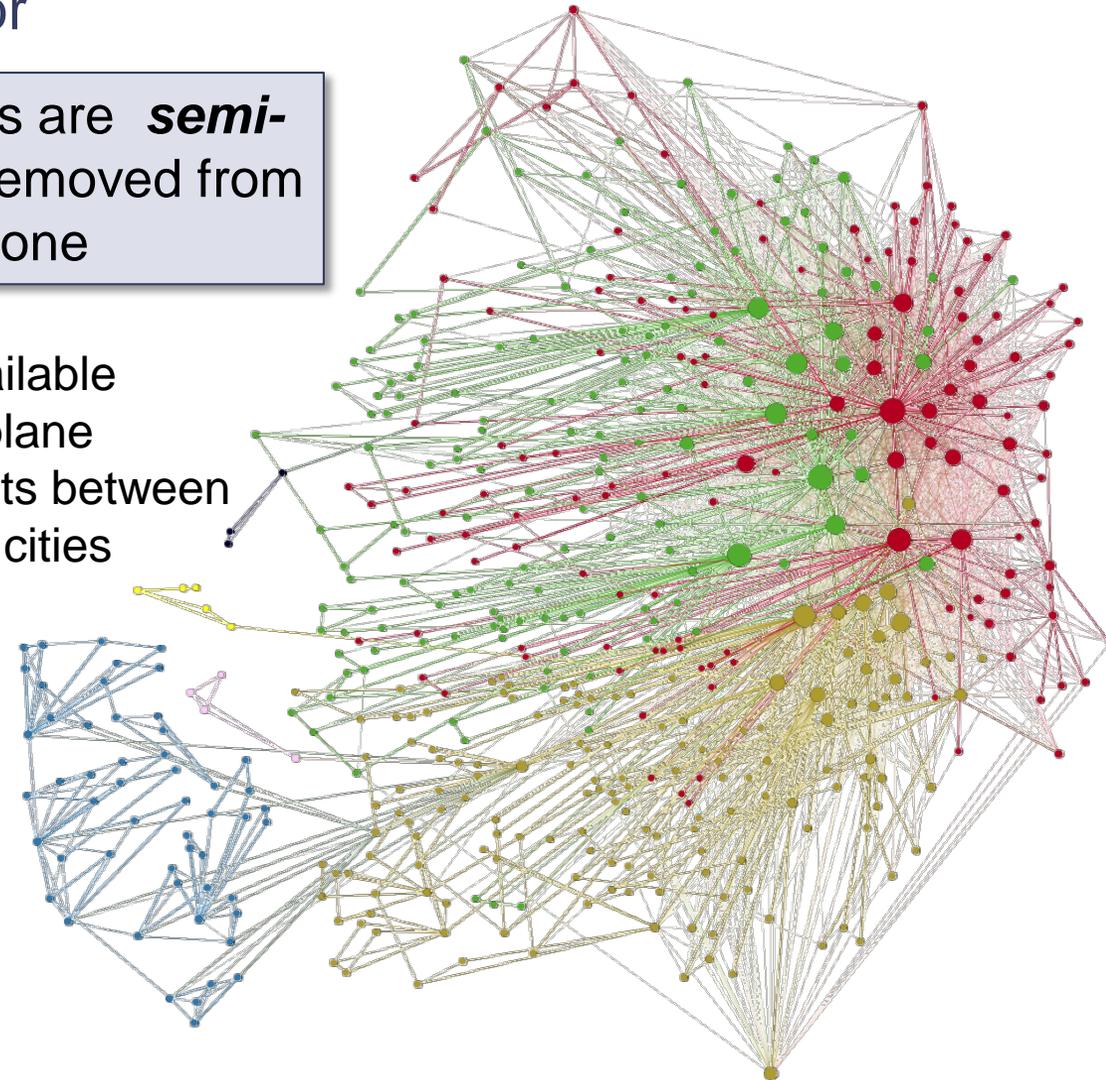
Invariant subgraph under metric closure (or APSP)

75% of edges are **semi-metric** and removed from metric backbone



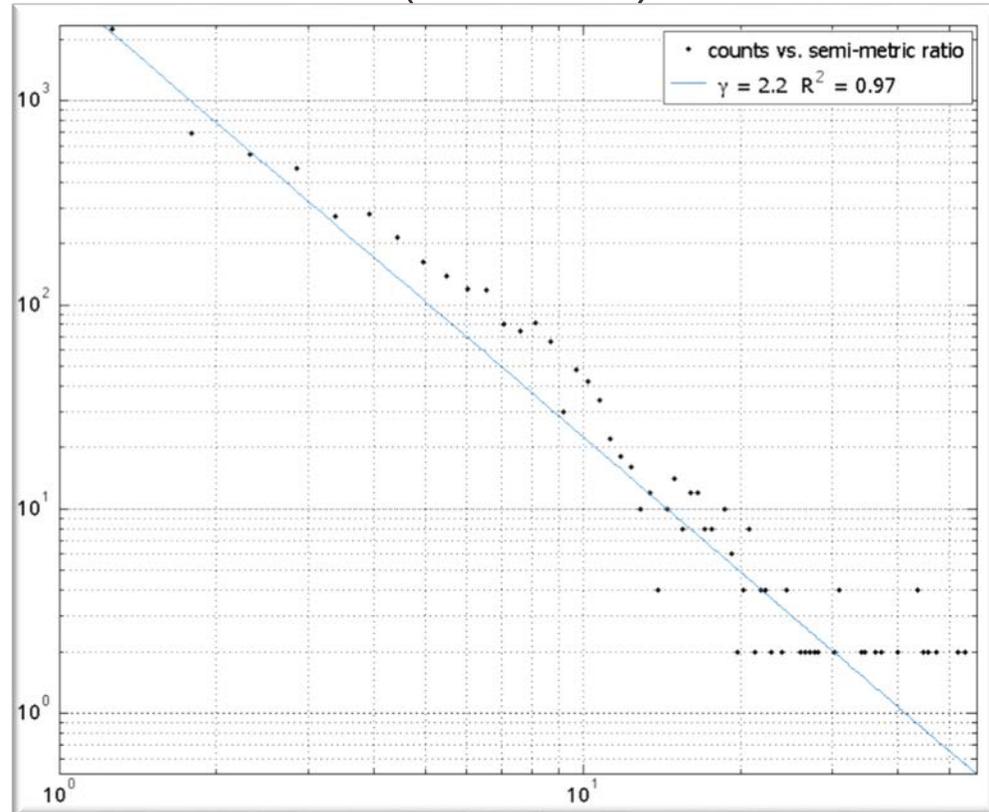
all pairs **shortest paths** problem (APSP) on distance graphs

Available airplane seats between US cities



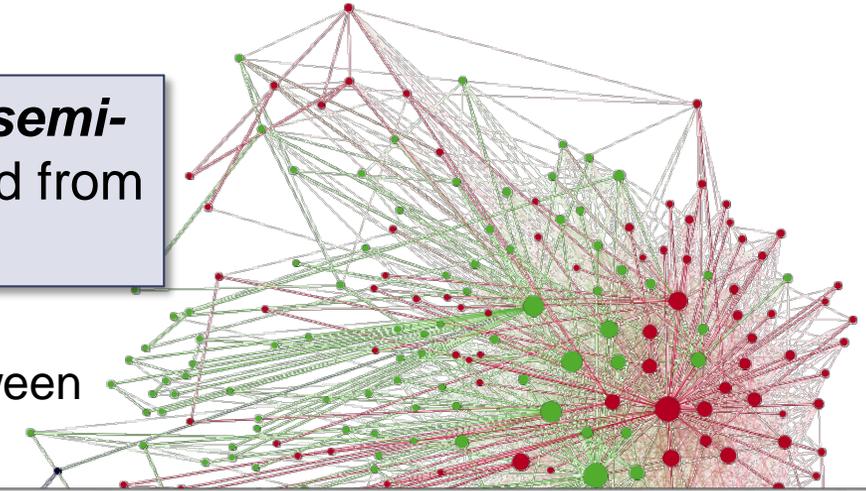
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Metric (distance) Backbone: minimum sub-graph for which all shortest paths are preserved.
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airplane seats between US cities

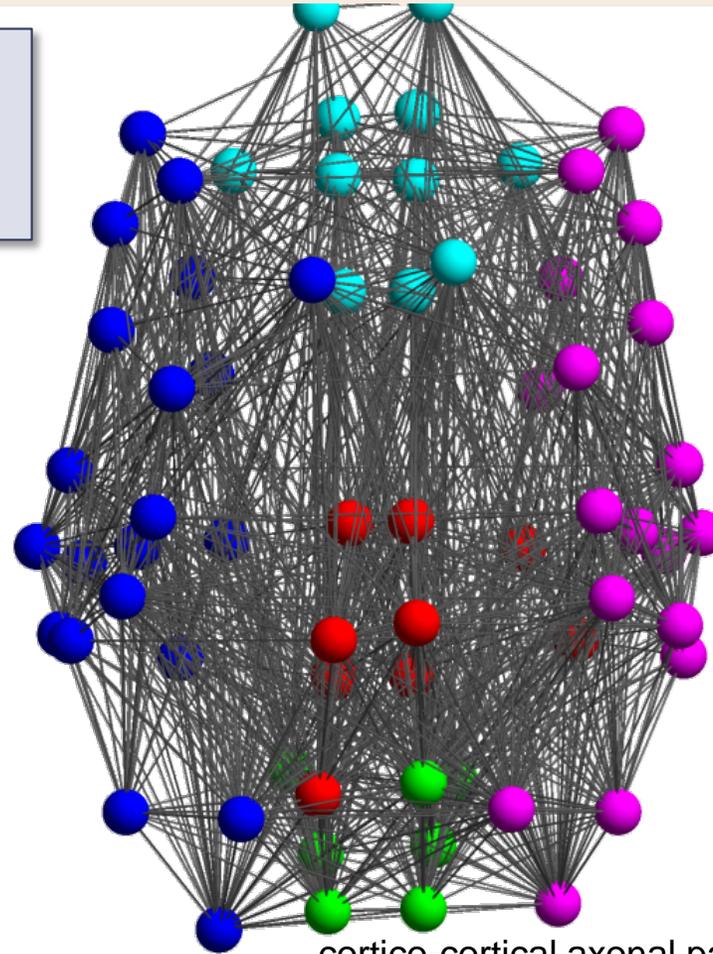


- **Semi-metric (semi-triangular) edges:**
 - Redundant for shortest-path computation (distance closure)
 - Null edge betweenness centrality
 - Varying *semi-metric distortion*
 - Participate in Clustering coefficient, Degree, Modularity
 - Do not form bridges
- **Metric (triangular) Edges:**
 - Participate in shortest path, Efficiency, betweenness
 - All bridges in metric backbone
- **Networks**
 - more semi-metric (redundant) early in evolution
 - semimetric networks robust to random node removal

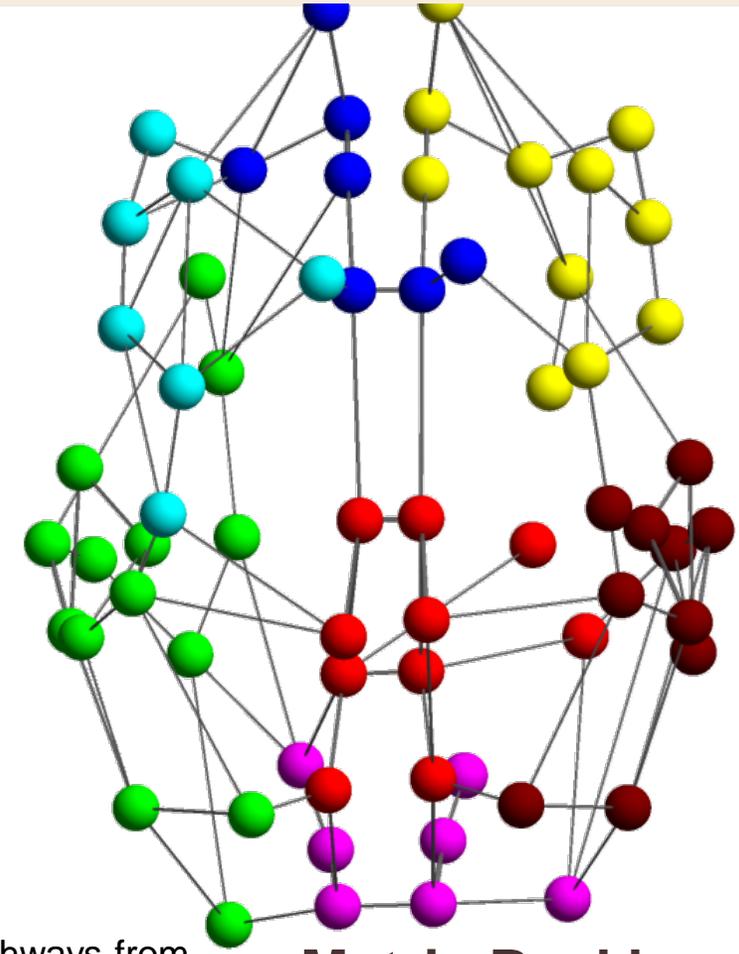
In brain, bio, and socio-technical distance networks

91% of edges are semi-metric (removed from backbone)

#id	Network	# Nodes	SM
1	USN	500	75%
2	HCN	66	91%
3	HBFN	116	85%
4	C-Elegans	297	31%
5	BKF	58	85%
6	ARP-IPP	1,702	71%
7	ARP-PIP	382	73%
8	ARP-Keywords	500	96%
9	WordNet	150	85%
10	SCN	12,722	9%
11	APN	14,845	20%
12	HEN	5,835	13%



cortico-cortical axonal pathways from diffusion spectrum Imaging (DSI)
Hagmann et al. [2008]. *PLoS Biol* 6(7): e159.



Metric Backbone

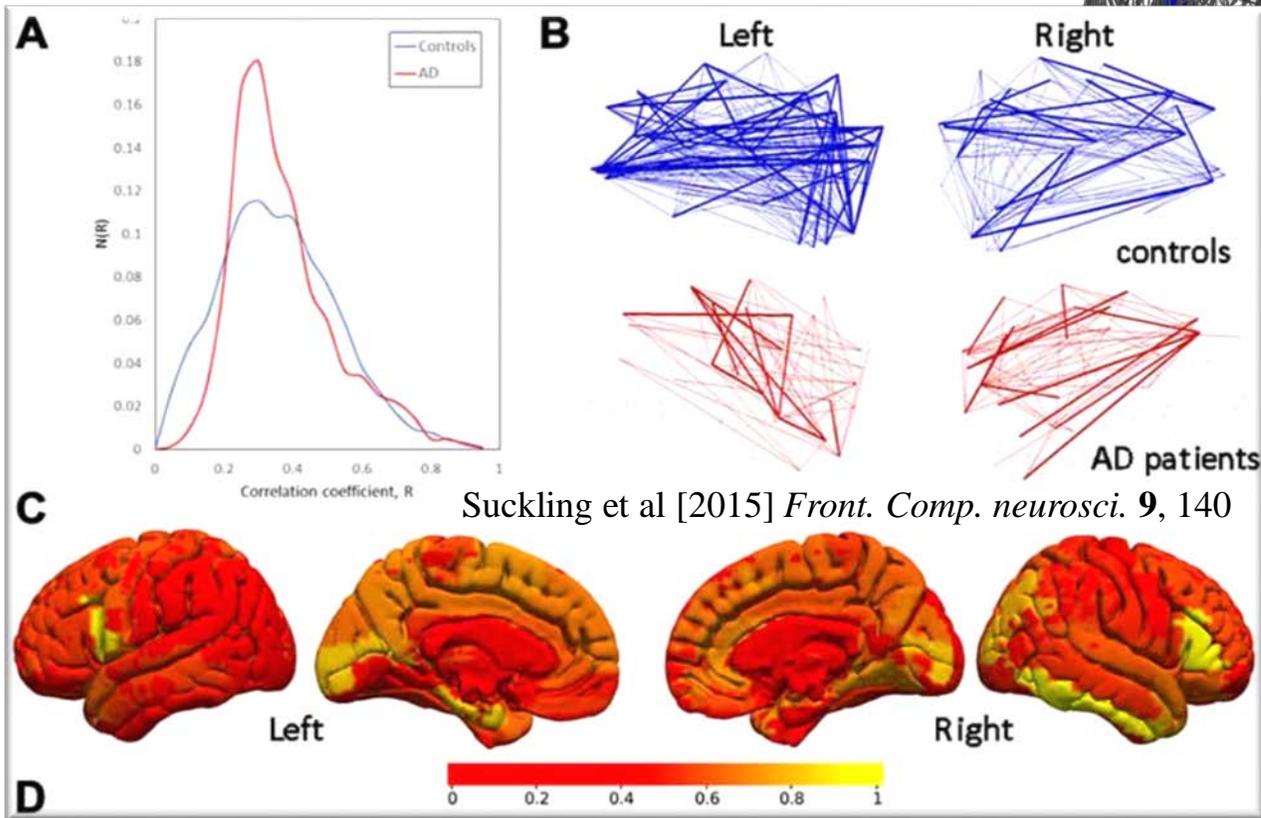
Simas, T. [2012]. *PhD Thesis*. Indiana University.

Simas & Rocha [2015]. *Network Science*. doi:10.1017/nws.2015.11

Simas, Ciampaglia, Correia, Sporns & Rocha [2018]. In Preparation.

In brain, bio, and socio-technical distance networks

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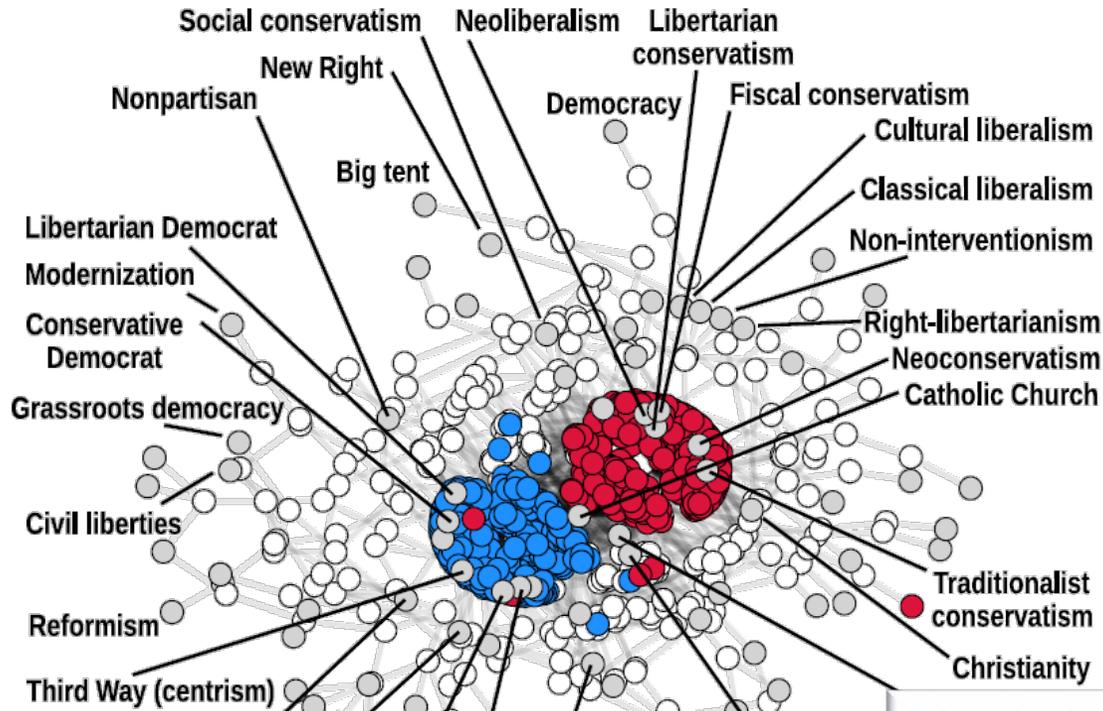


discriminates Alzheimer's and Autism patients from healthy subjects

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Metric Backbone

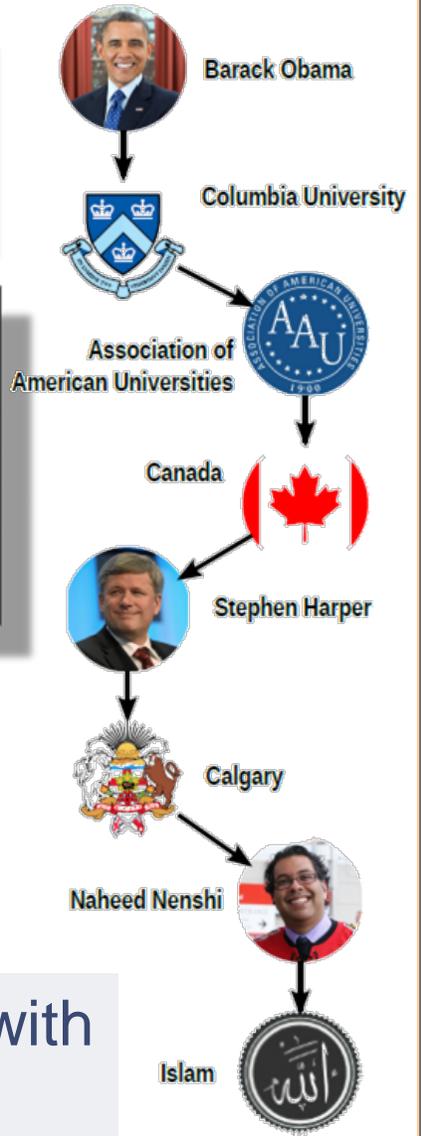
from data in Wikipedia



Massive distance graph
 3.14 Million nodes
 23 Million edges

Fact-Checking
 Associative inference via shortest paths (metric backbone) of maximum Information content distance/knowledge graph

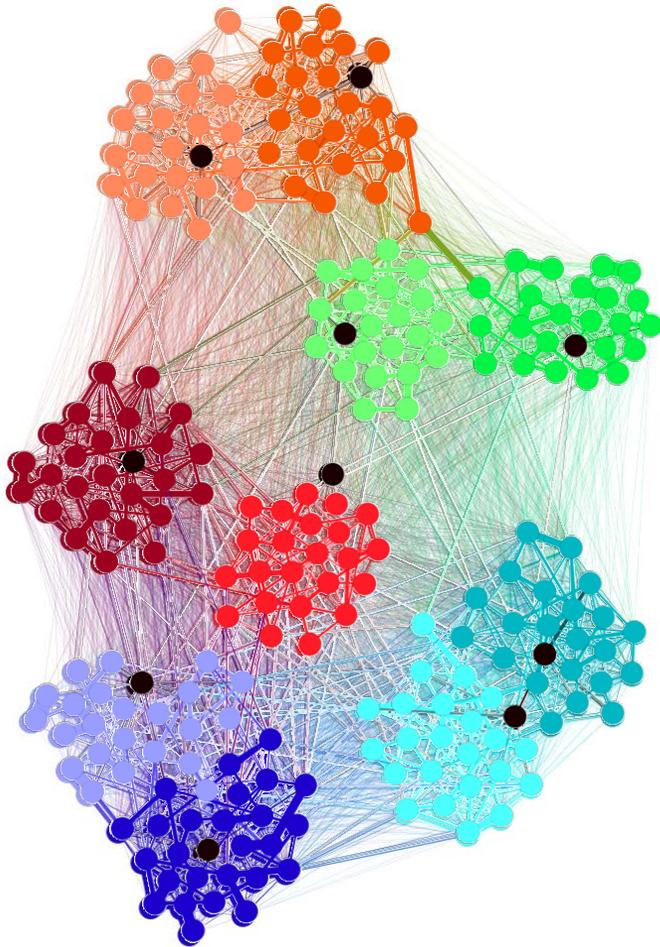
Metric backbone is 2% of knowledge graph



4.0 million "things" with 470 million "facts".

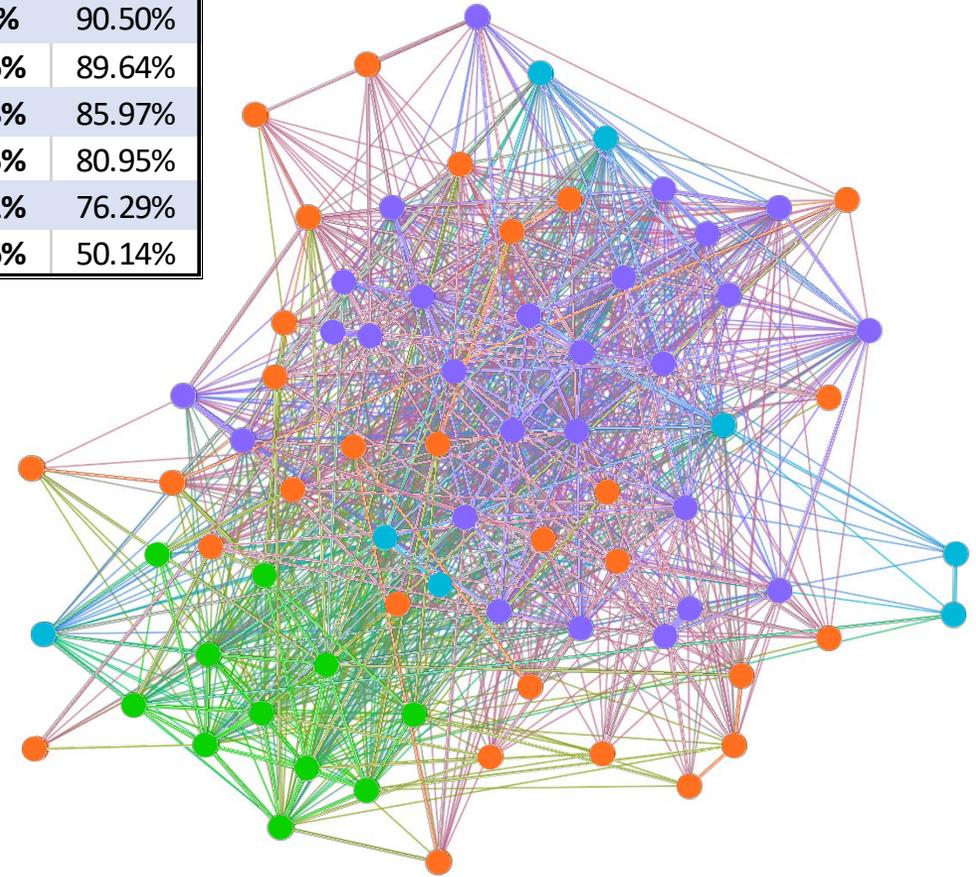
on social contact distance networks

Network	N	E	Con	MB	SM
Primary School	242	8317	28.52%	9.50%	90.50%
High School	327	5818	10.92%	10.36%	89.64%
Conference	113	2196	34.70%	14.03%	85.97%
Hospital	75	1139	41.05%	19.05%	80.95%
workplace	92	755	18.04%	23.71%	76.29%
Museum	200	714	3.59%	49.86%	50.14%



metric backbone
sufficient to compute all
shortest paths

Does it preserve social
organization in
SocioPatterns datasets?



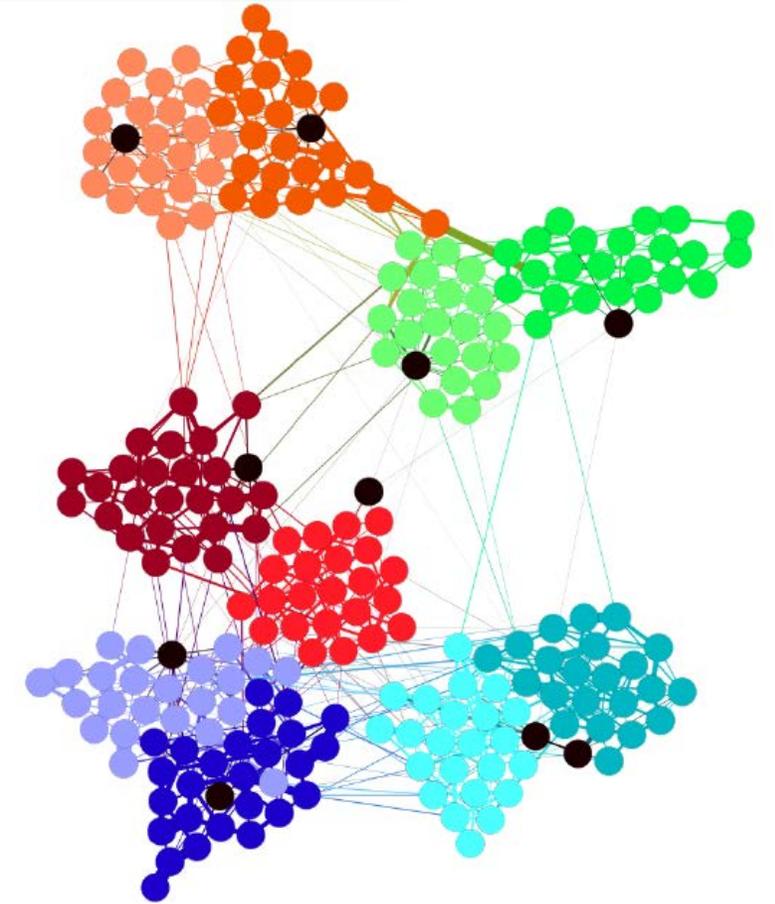
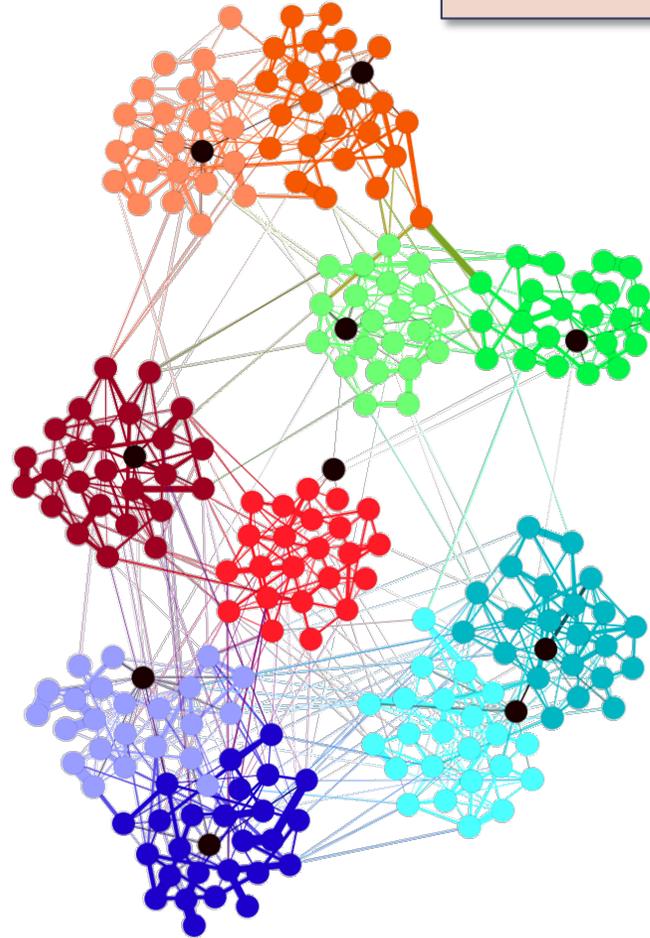
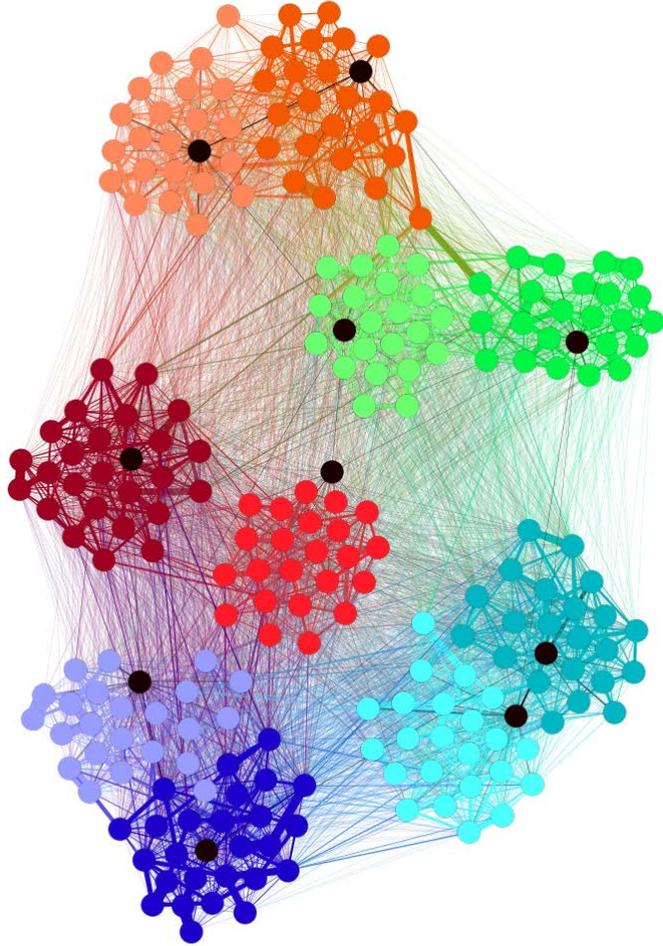
SocioPatterns

R. Mastrandrea, J. Fournet, A. Barrat, *PLoS ONE*
10(9):e0136497 (2015)

is preserved in metric backbone

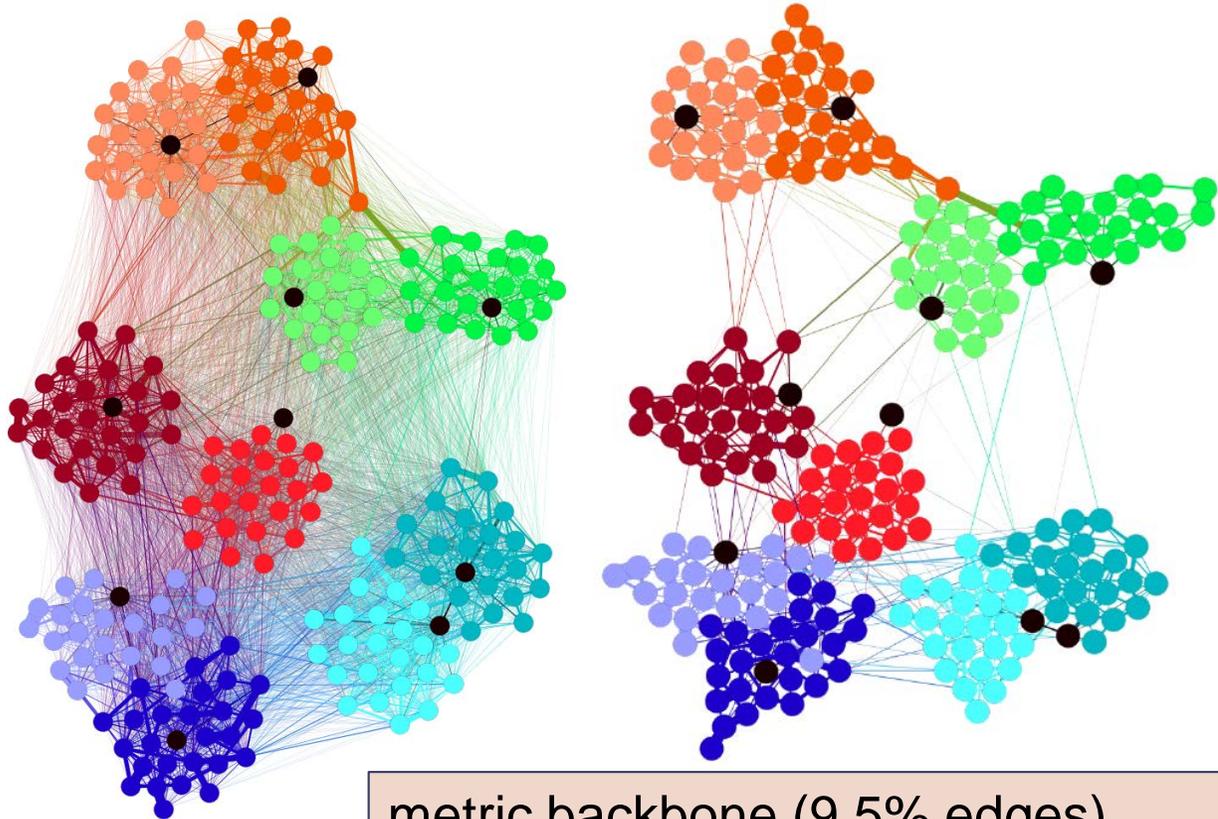
Network	N	E	Con	MB	SM
Primary School	242	8317	28.52%	9.50%	90.50%

Original class labels remain as communities in metric backbone subgraph

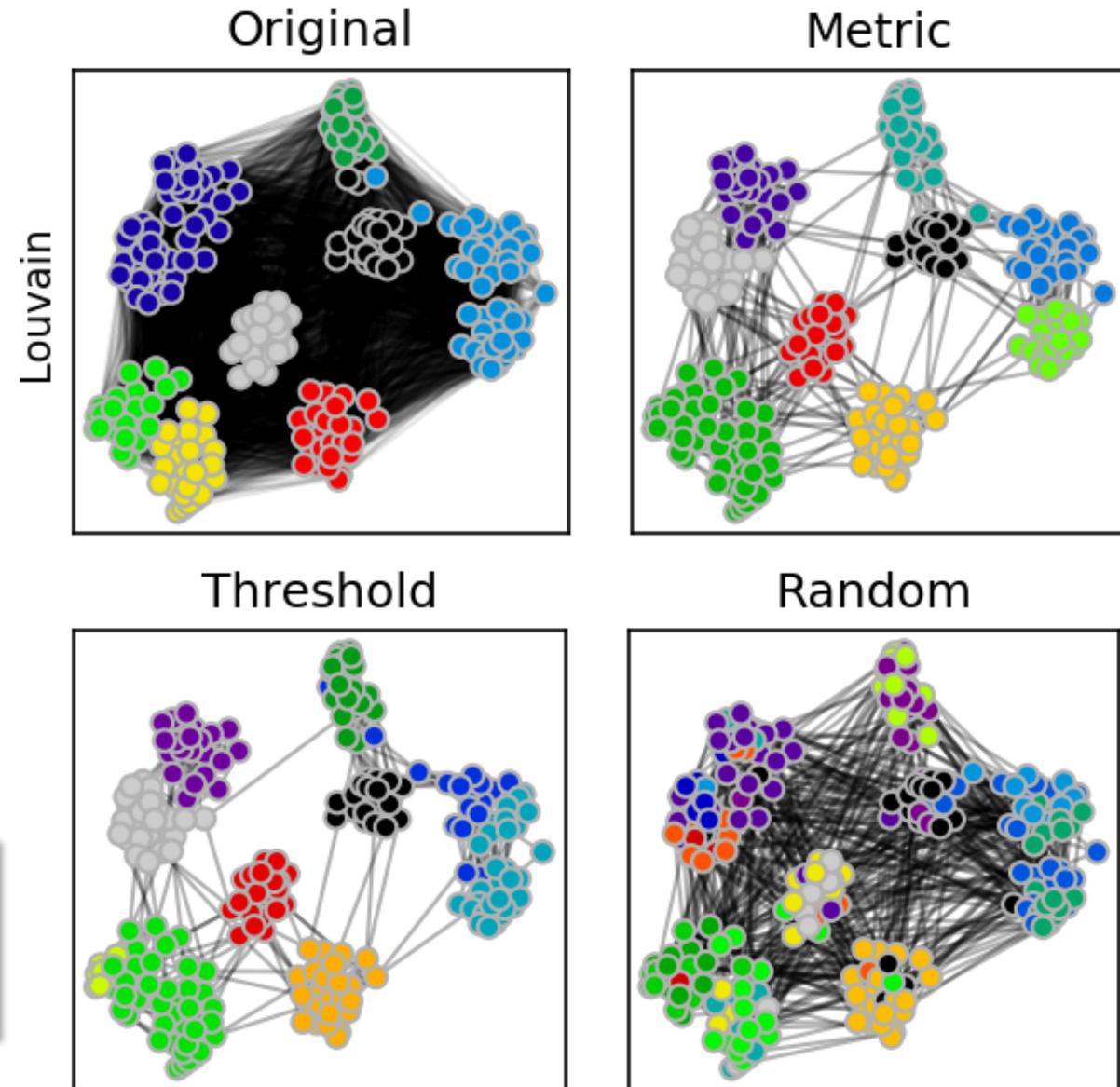


metric backbone vs. distance threshold and random deletion “backbones” of same size

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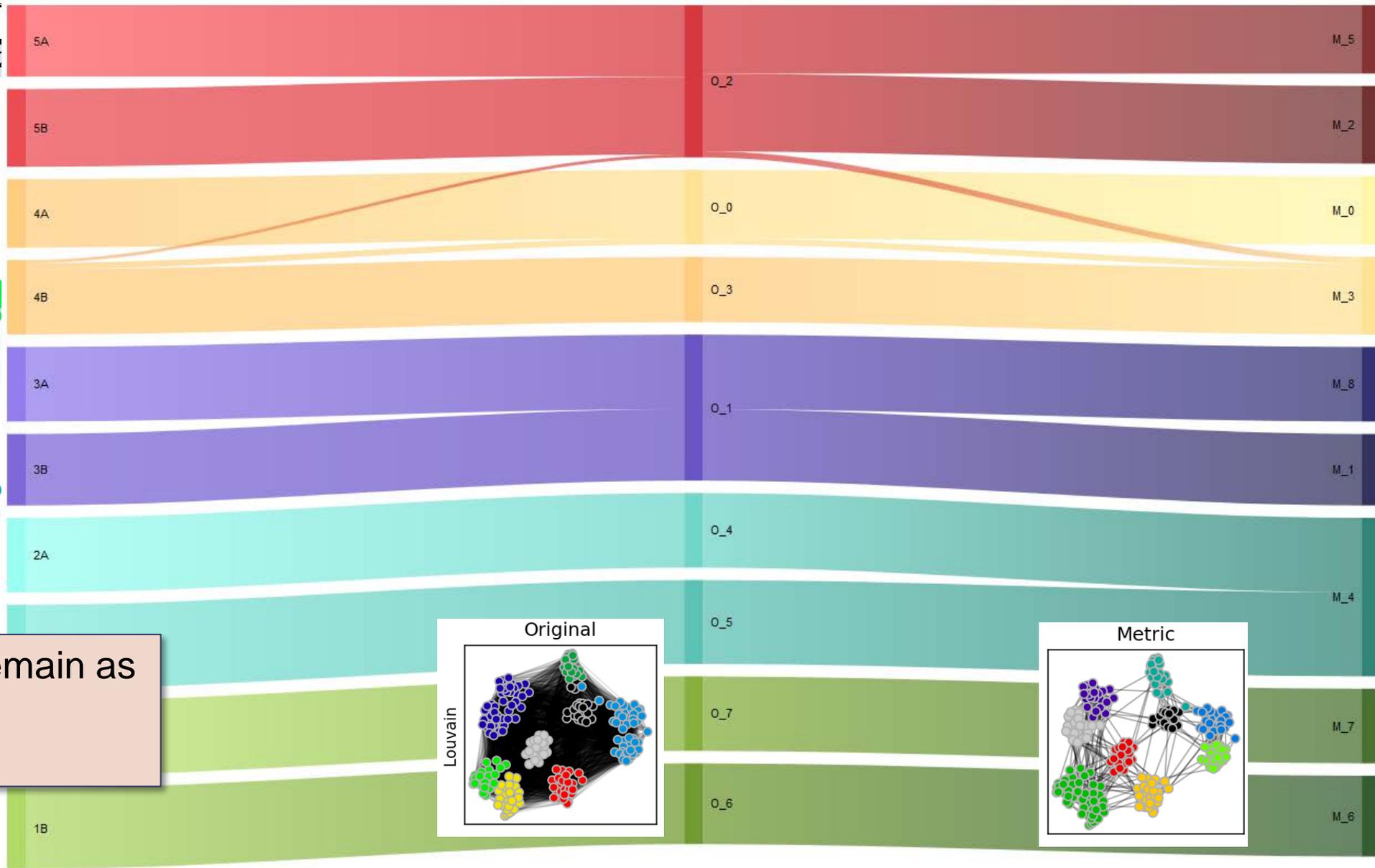
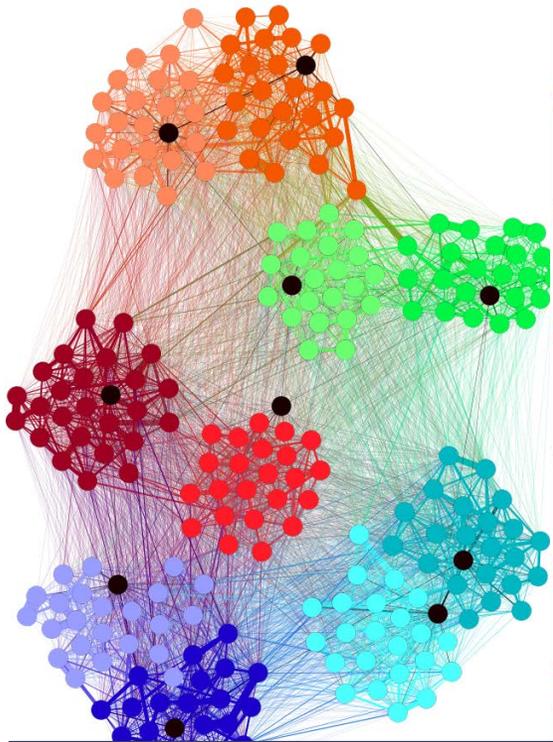
metric backbone (9.5% edges)
sufficient to compute all shortest
paths unlike other “backbones”



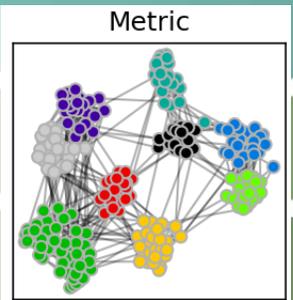
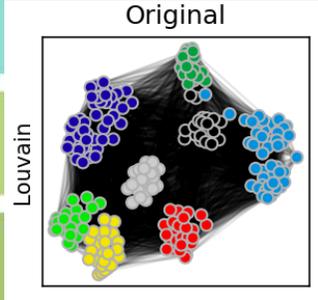
community structure of primary school contact network

metric backbone vs. distance threshold and random deletion “backbones” of same size

Network	N	E
Primary School	242	8317



original class labels remain as communities in metric backbone subgraph



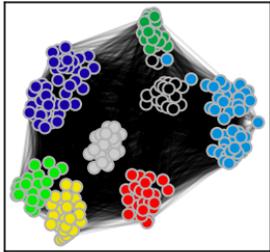
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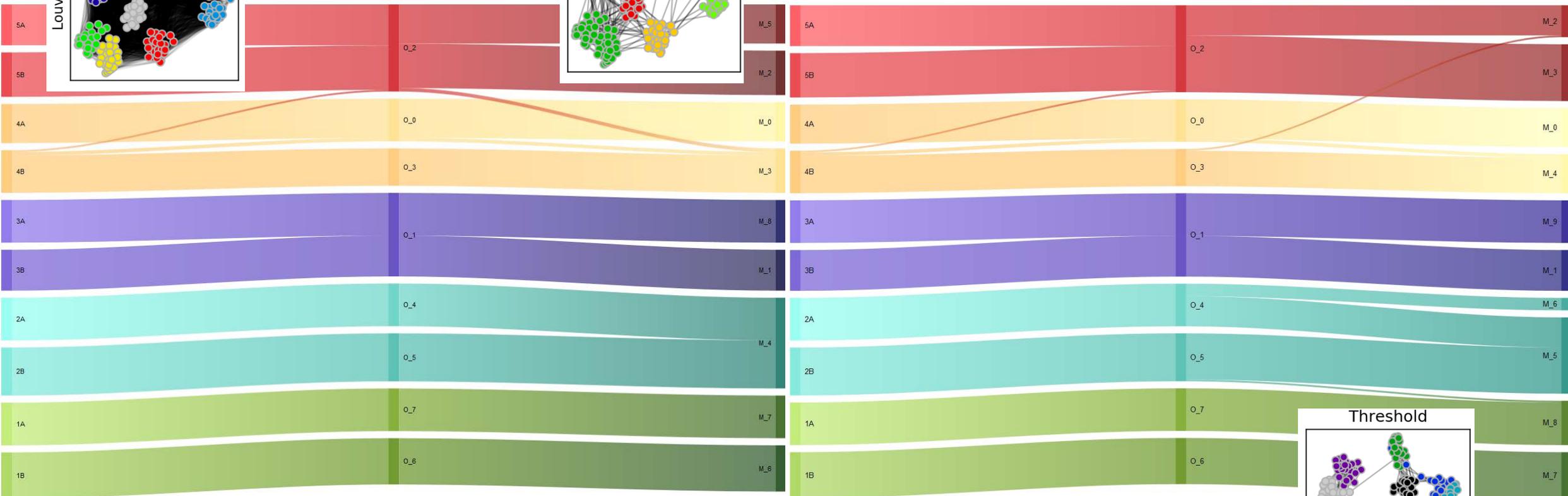
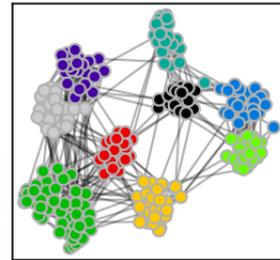
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Network	Communities				
	metalabels	Louvain			
	---	Original	Metric	Threshold	Random
Primary	10	8	9	10	21.15(±2.23)

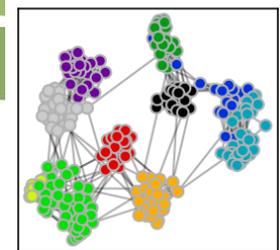
Original



Metric



Threshold



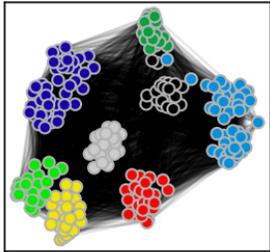
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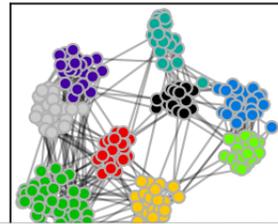
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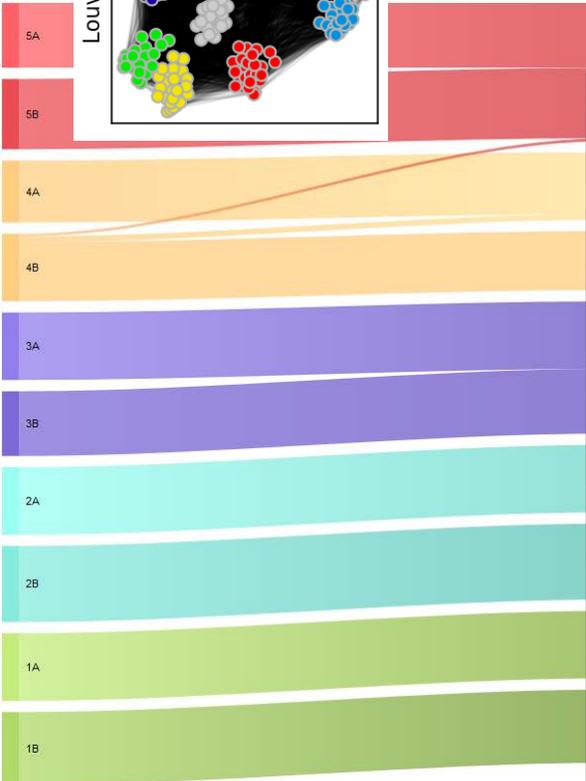
Original



Metric



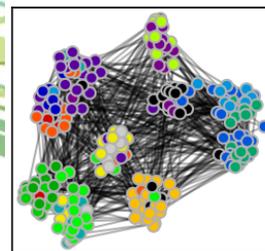
Louvain



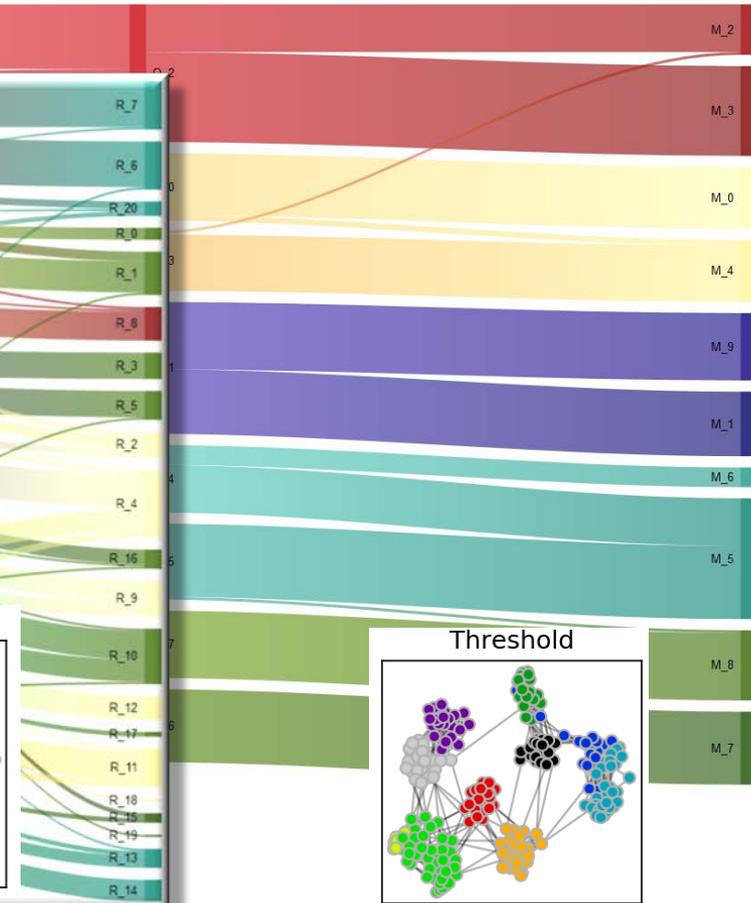
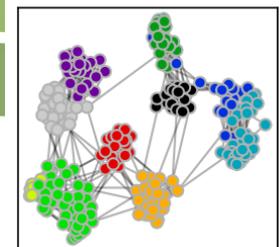
Metric backbone preserves social structure better (as quantified by information theoretical measures) in SocioPatterns datasets

metric backbone (9.5% edges) sufficient to compute all shortest paths unlike other “backbones”

Random



Threshold



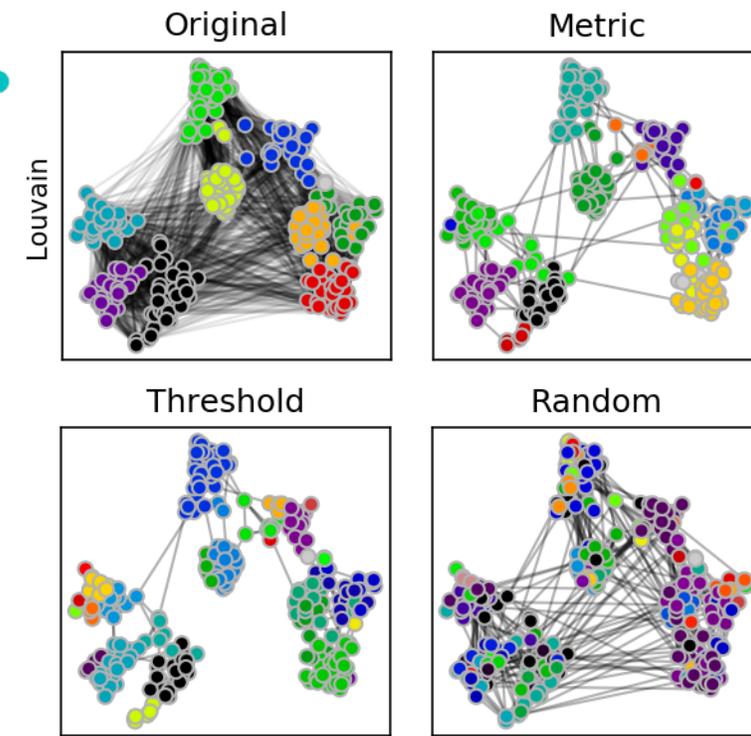
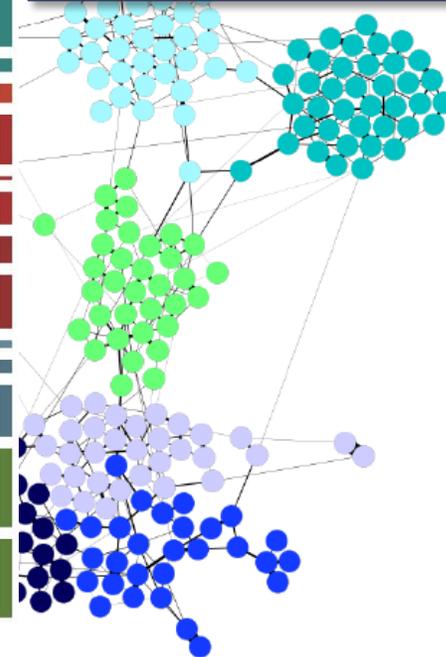
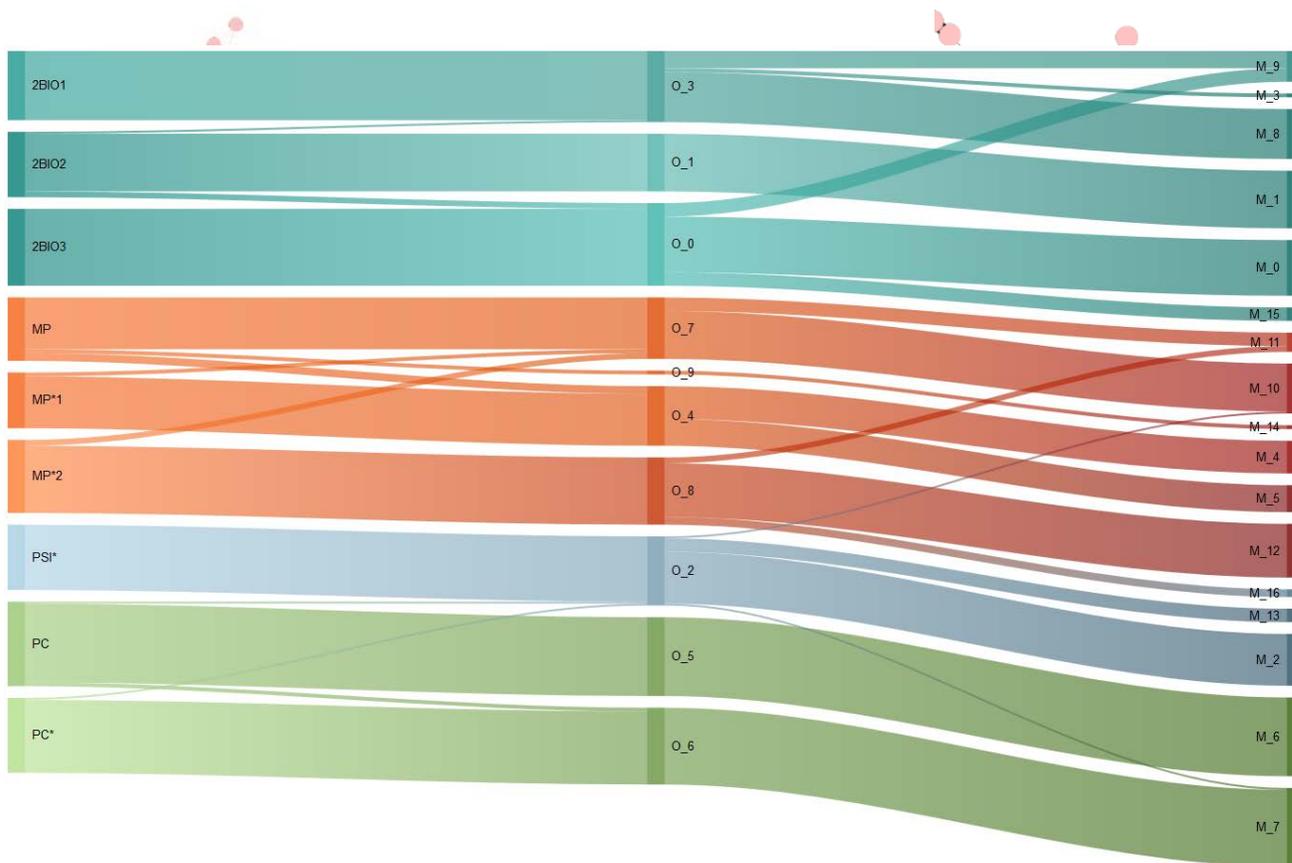
community structure of high school contact network

metric backbone vs. distance threshold and random deletion “backbones” of same size

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Original class labels and community structure remain as communities in metric backbone subgraph despite appearance of a few smaller, nested communities

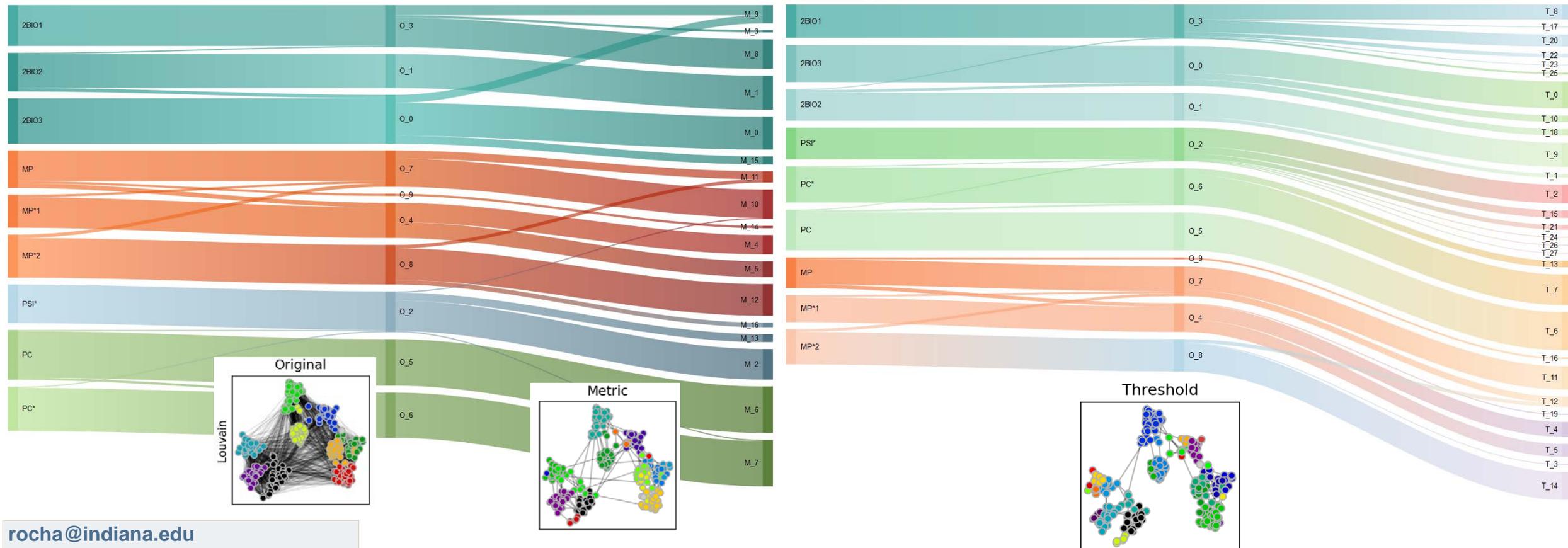


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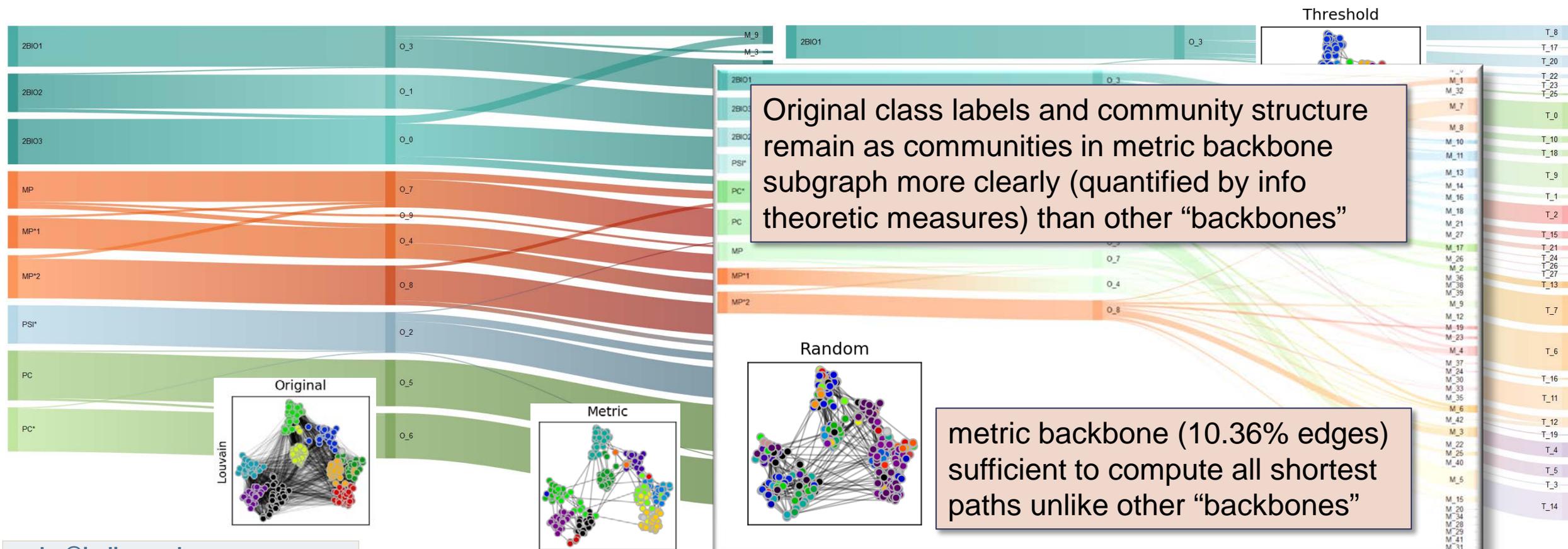


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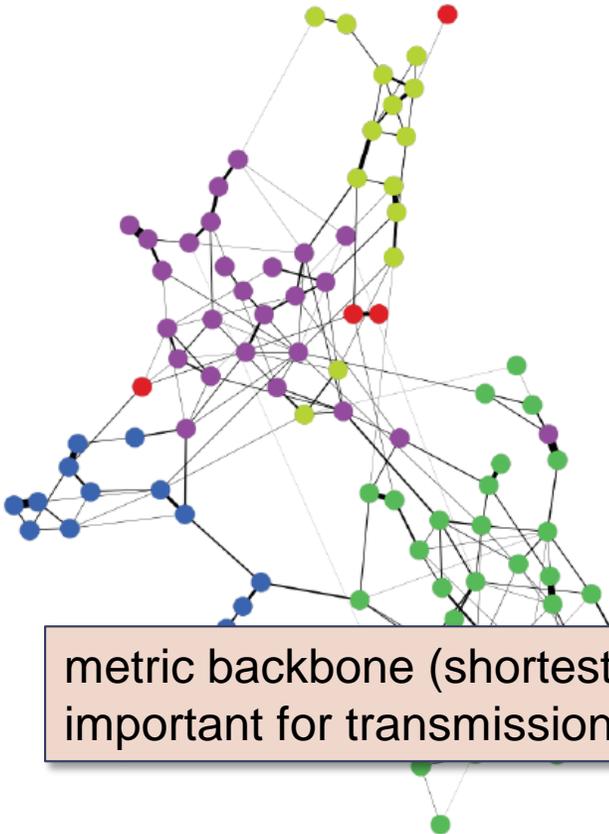
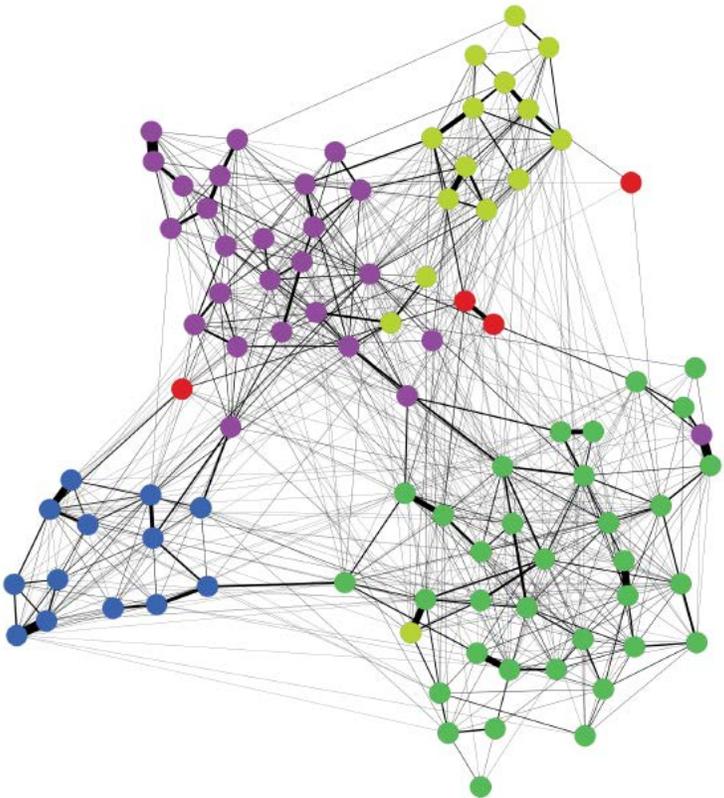
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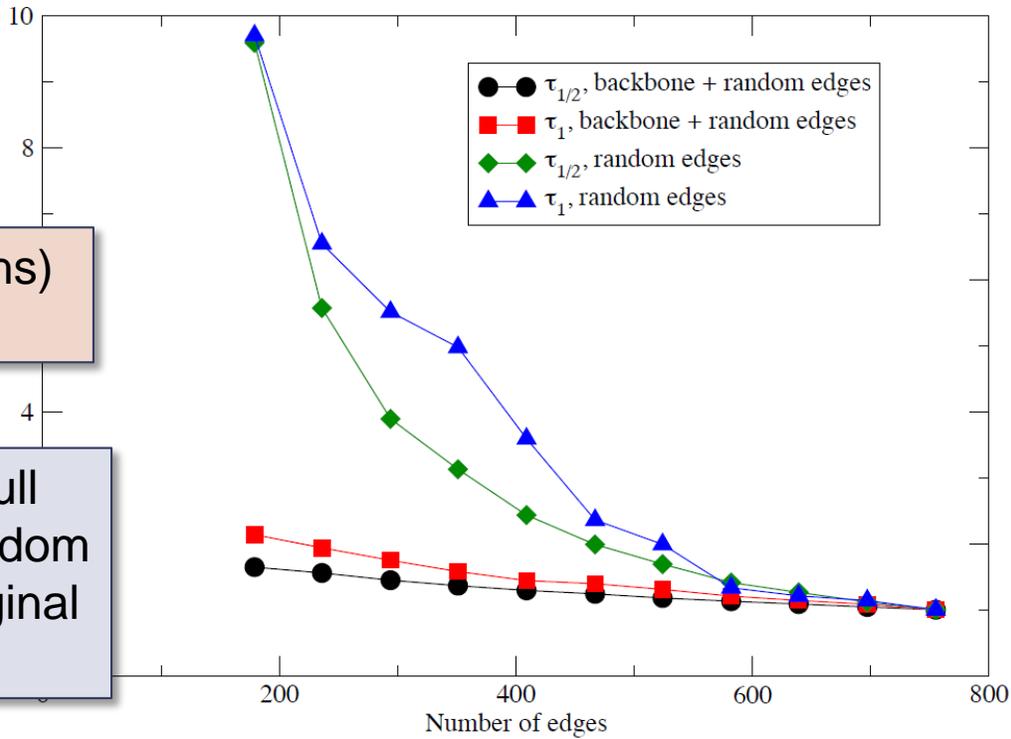
preliminary results



metric backbone (shortest paths) important for transmission

SI processes. Time to 1/2 and full infection on backbone and random "backbone" as edges from original network are added

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SocioPatterns

<http://bit.ly/SMNets>

MERCI!
THANK YOU!
OBRIGADO!